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**Math 5520, Winter 2009, Homework 1**  
**12 January 2009**  
**(due 16 January 2009)**

1. Find a continuous function with continuous inverse from the open interval  $(-1, 1)$  to the real line  $\mathbf{R}^1$ . Give formulas for both the function and its inverse.
2. Find a continuous function with continuous inverse from the standard 2-disk  $D^2$  to the square  $[-1, 1] \times [-1, 1]$ . Hint, it is sufficient to do this for the quarter of a circle which lies within  $45^\circ$  of the positive  $x$ -axis, and then repeat it in each of the other 3 quadrants.
3. Complete the classification of regular polyhedra begun in class (and in section 1 of the text), as follows. For each possible value of
  - $a$  = number of edges per face, and
  - $b$  = number of edges per vertex,

compute  $V$ ,  $E$ ,  $F$  to satisfy Euler's formula  $V - E + F = 2$  and identify the corresponding polyhedron from Figure 1.9 or state that no such polyhedron exists.

	$a = 3$	$a = 4$	$a = 5$	$a = 6$
$b = 3$	$E = 6$ $V = F = 4$ tetrahedron			Impossible
$b = 4$				
$b = 5$				
$b = 6$				

4. Problem 10 on page 11. Can you see a geometric explanation of this duality?
5. Compute the Euler characteristics of the complexes in Figure 13 on page 4.