

Name: _____

Math 2250, Fall 2011, Quiz 9

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Answer 'Y' (yes) or 'N' (no) to each of the following.
Use the usual addition and scalar multiplication in each.

Are these vector spaces?

___ $\left\{ \begin{bmatrix} x \\ y \end{bmatrix} \mid 2x + 3y = 0 \right\}$

___ $\left\{ \begin{bmatrix} x \\ y \end{bmatrix} \mid 2x + 3y = 5 \right\}$

___ $\left\{ \begin{bmatrix} 2a + 3b \\ a - b \end{bmatrix} \mid a, b \text{ real} \right\}$

___ Polynomials of the form $ax^5 + bx^3 + cx^2$, with a, b and c real.

___ Degree 4 polynomials whose value at 1 is 0.

___ Degree 4 polynomials whose value at 1 is 1.

Are these linear transformations?

___ $T : \mathbf{R}^2 \rightarrow \mathbf{R}^2$ by $T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} x + y \\ xy \end{bmatrix}$.

___ $T : \mathbf{R}^2 \rightarrow \mathbf{R}^2$ by $T\left(\begin{bmatrix} x \\ y \end{bmatrix}\right) = \begin{bmatrix} 2x + y \\ x - y \end{bmatrix}$.

___ $T : P_4 \rightarrow \mathbf{R}^2$ by $T(p) = \begin{bmatrix} p(1) \\ p(2) \end{bmatrix}$.

___ $T : P_4 \rightarrow P_3$ by $T(p) = p' - p(2)$.