R. Bruner Math 2150, Fall 2005, Quiz 10 November 9, 2005

The functions

$$y_1 = e^{3t} \begin{bmatrix} 1\\1\\1 \end{bmatrix}, \qquad y_2 = e^{2t} \begin{bmatrix} 1\\0\\0 \end{bmatrix}, \qquad y_3 = e^{-t} \begin{bmatrix} 1\\1\\0 \end{bmatrix}$$
solve the differential equation
$$y' = \begin{bmatrix} 2 & -3 & 4\\0 & -1 & 4\\0 & 0 & 3 \end{bmatrix} y.$$

(You do not need to check this.)

- 1. Show that they form a fundamental solution set.
- 2. Find the solution which satisfies

$$y(0) = \left[\begin{array}{c} 1\\ 2\\ 3 \end{array} \right].$$