

(There are many solutions. This is one.)

3. Subdivide $[1, 3]$ into 4 equal pieces at $\frac{3}{2}, 2, \frac{5}{2}$ and use midpoints $\frac{5}{4}, \frac{7}{4}, \frac{9}{4}$ and $\frac{11}{4}$.

$$f\left(\frac{5}{4}\right)\left(\frac{3}{2}-1\right) + f\left(\frac{7}{4}\right)\left(2-\frac{3}{2}\right) + f\left(\frac{9}{4}\right)\left(\frac{5}{2}-2\right) + f\left(\frac{11}{4}\right)\left(3-\frac{5}{2}\right)$$
$$= \frac{4}{5} \cdot \frac{1}{2} + \frac{4}{7} \cdot \frac{1}{2} + \frac{4}{9} \cdot \frac{1}{2} + \frac{4}{11} \cdot \frac{1}{2}$$

$$= \frac{2}{5} + \frac{2}{7} + \frac{2}{9} + \frac{2}{11} = \frac{3776}{3465} \approx 1.08$$

Riemann sum for

$$\int_1^3 \frac{1}{x} dx$$

4. $\int_1^2 f(x) dx = \int_1^5 f(x) dx - \int_2^5 f(x) dx = 10 - 8 = \boxed{2}$

5. $\int_1^3 f(x) - 2g(x) dx = \int_1^3 f(x) dx - 2 \int_1^3 g(x) dx = 7 - 2(4) = \boxed{-1}$

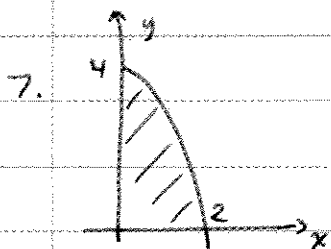
6. Increasing \Rightarrow left end underestimates, right overestimates.

$$\text{Under} = f(0)(3-0) + f(3)(5-3) + f(5)(8-5) + f(8)(10-8)$$
$$= 1(3) + 2(2) + 4(3) + 5(2)$$

$$= 3 + 4 + 12 + 10 = \boxed{29}$$

$$\text{Over} = f(3)(3-0) + f(5)(5-3) + f(8)(8-5) + f(10)(10-8)$$
$$= 2(3) + 4(2) + 5(3) + 8(2)$$

$$= 6 + 8 + 15 + 16 = \boxed{45}$$



$$\text{Area} = \int_0^2 4 - x^2 dx = 4x - \frac{x^3}{3} \Big|_0^2 = 8 - \frac{8}{3} = \boxed{\frac{16}{3}}$$